Package 'dcortools'

December 9, 2025

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Title Providing Fast and Flexible Functions for Distance Correlation Analysis	
Description Provides methods for distance covariance and distance correlation (Szekely, et al. (2007) <doi:10.1214 009053607000000505="">), generalized version thereof (Sejdinovic, et al. (2013) <doi:10.1214 13-aos1140="">) and corresponding tests (Berschneider, Bottcher (2018) <doi:10.48550 arxiv.1808.07280="">. Distance standard deviation methods (Edelmann, et al. (2020) <doi:10.1214 19-aos1935="">) and distance co relation methods for survival endpoints (Edelmann, et al. (2021) <doi:10.1111 biom.13470="">) are also included.</doi:10.1111></doi:10.1214></doi:10.48550></doi:10.1214></doi:10.1214>	r-
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dcmatrix

Calculates distance covariance and distance correlation matrices

Description

Calculates distance covariance and distance correlation matrices

Usage

```
dcmatrix(
 Χ,
  Y = NULL,
 calc.dcov = TRUE,
  calc.dcor = TRUE,
  calc.cor = "none",
  calc.pvalue.cor = FALSE,
  return.data = TRUE,
  test = "none",
  adjustp = "none",
 b = 499,
 affine = FALSE,
  standardize = FALSE,
 bias.corr = FALSE,
  group.X = NULL,
  group.Y = NULL,
 metr.X = "euclidean",
 metr.Y = "euclidean",
 use = "all",
  algorithm = "auto",
  fc.discrete = FALSE,
  calc.dcor.pw = FALSE,
  calc.dcov.pw = FALSE,
  test.pw = "none",
 metr.pw.X = "euclidean",
 metr.pw.Y = "euclidean"
)
```

Arguments

metr.Y

use

see metr.X.

Χ A data.frame or matrix. Υ Either NULL or a data frame or a matrix with the same number of rows as X. If only X is provided, distance covariances/correlations are calculated between all groups in X. If X and Y are provided, distance covariances/correlations are calculated between all groups in X and all groups of Y. calc.dcov logical; specifies if the distance covariance matrix is calculated. calc.dcor logical; specifies if the distance correlation matrix is calculated. calc.cor If set as "pearson", "spearman" or "kendall", a corresponding correlation matrix is additionally calculated. calc.pvalue.cor logical; IF TRUE, a p-value based on the Pearson or Spearman correlation matrix is calculated (not implemented for calc.cor ="kendall") using Hmisc::rcorr. return.data logical; specifies if the dematrix object should contain the original data. specifies the type of test that is performed, "permutation" performs a Monte test Carlo Permutation test. "gamma" performs a test based on a gamma approximation of the test statistic under the null. "conservative" performs a conservative two-moment approximation. "bb3" performs a quite precise three-moment approximation and is recommended when computation time is not an issue. If setting this parameter to "holm", "hochberg", "hommel", "bonferroni", "BH", adjustp "BY" or "fdr", corresponding adjusted p-values are additionally returned for the distance covariance test. b specifies the number of random permutations used for the permutation test. Ignored for all other tests. affine logical; indicates if the affinely transformed distance covariance should be calculated or not. specifies if data should be standardized dividing each component by its standard standardize deviations. No effect when affine = TRUE. bias.corr logical; specifies if the bias corrected version of the sample distance covariance (Huo and Szekely 2016) should be calculated. group.X A vector, each entry specifying the group membership of the respective column in X. Each group is handled as one sample for calculating the distance covariance/correlation matrices. If NULL, every sample is handled as an individual group. group.Y A vector, each entry specifying the group membership of the respective column in Y. Each group is handled as one sample for calculating the distance covariance/correlation matrices. If NULL, every sample is handled as an individual metr.X Either a single metric or a list providing a metric for each group in X (see examples).

"all" uses all observations, "complete.obs" excludes NAs, "pairwise.complete.obs"

uses pairwise complete observations for each comparison.

algorithm specifies the algorithm used for calculating the distance covariance. "fast" uses an O(n log n) algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely (2016)."memsave" uses a memory saving version of the standard algorithm with computational complexity $O(n^2)$ but requiring only O(n) memory. "standard" uses the classical algorithm. User-specified metrics always use the classical algorithm. "auto" chooses the best algorithm for the specific setting using a rule of thumb. "memsave" is typically very inefficient for dcmatrix and should only be applied in exceptional cases. logical; If TRUE, "discrete" metric is applied automatically on samples of type fc.discrete "factor" or "character". logical; If TRUE, a distance correlation matrix between the univariate observacalc.dcor.pw tions/columns is additionally calculated. Not meaningful if group.X and group.Y are not specified. calc.dcov.pw logical; If TRUE, a distance covariance matrix between the univariate observations/columns is additionally calculated. Not meaningful if group.X and group.Y are not specified. specifies a test (see argument "test") that is performed between all single obsertest.pw vations. metr.pw.X Either a single metric or a list providing a metric for each single observation/column

Value

metr.pw.Y

S3 object of class "dcmatrix" with the following components

in X (see metr.X).

See metr.pw.Y.

name X, Y description original data (if return.data = TRUE).

name dcov, dcor distance covariance/correlation matrices between the groups specified in group.X/group.Y

(if calc.dcov/calc.dcor = TRUE).

name corr correlation matrix between the univariate observations/columns (if cal.cor is

"pearson", "spearman" or "kendall").

name pvalue matrix of p-values based on a corresponding distance covariance test based on

the entries in dcov (if argument test is not "none").

name pvalue.adj

matrix of p-values adjusted for multiple comparisons using the method specified

in argument adjustp.

name pvalue.cor

matrix of pvalues based on "pearson"/"spearman" correlation (if calc.cor is "pear-

son" or "spearman" and calc.pvalue.cor = TRUE).

name dcov.pw, dcor.pw

distance covariance/correlation matrices between the univariate observations (if

calc.dcov.pw/calc.dcor.pw = TRUE.)

name pvalue.pw matrix of p-values based on a corresponding distance covariance test based on

the entries in dcov.pw (if argument test is not "none").

References

Berschneider G, Bottcher B (2018). "On complex Gaussian random fields, Gaussian quadratic forms and sample distance multivariance." *arXiv preprint arXiv:1808.07280*.

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*, **20**, 2305–2330.

Huang C, Huo X (2017). "A statistically and numerically efficient independence test based on random projections and distance covariance." *arXiv preprint arXiv:1701.06054*.

Huo X, Szekely GJ (2016). "Fast computing for distance covariance." *Technometrics*, **58**(4), 435–447.

Lyons R (2013). "Distance covariance in metric spaces." The Annals of Probability, 41, 3284–3305.

Sejdinovic D, Sriperumbudur B, Gretton A, Fukumizu K (2013). "Equivalence of distance-based and RKHS-based statistics in hypothesis testing." *The Annals of Statistics*, **41**, 2263–2291.

Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X \leftarrow matrix(rnorm(1000), ncol = 10)
dcm <- dcmatrix(X, test="bb3",calc.cor = "pearson",</pre>
 calc.pvalue.cor = TRUE, adjustp = "BH")
dcm <- dcmatrix(X, test="bb3",calc.cor = "pearson",</pre>
 calc.pvalue.cor = TRUE, adjustp = "BH",
 group.X = c(rep(1, 5), rep(2, 5)),
 calc.dcor.pw = TRUE, test.pw = "bb3")
Y <- matrix(rnorm(600), ncol = 6)
Y[,6] \leftarrow rbinom(100, 4, 0.3)
dcm <- dcmatrix(X, Y, test="bb3",calc.cor = "pearson",</pre>
 calc.pvalue.cor = TRUE, adjustp = "BH")
dcm <- dcmatrix(X, Y, test="bb3",calc.cor = "pearson",</pre>
 calc.pvalue.cor = TRUE, adjustp = "BH",
 group.X = c(rep("group1", 5), rep("group2", 5)),
 group.Y = c(rep("group1", 5), "group2"),
 metr.X = "gaussauto",
 metr.Y = list("group1" = "gaussauto", "group2" = "discrete"))
```

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dcorgaussianbiv	Calculates distance correlation from Pearson correlation under as-
	sumption of a bivariate normal distribution

Description

Calculates distance correlation from Pearson correlation under assumption of a bivariate normal distribution

Usage

```
dcorgaussianbiv(rho)
```

Arguments

rho

Pearson correlation.

Value

Distance correlation assuming a bivariate normal distribution

dcsis

Performs distance correlation sure independence screening (Li et al. 2012) with some additional options (such as calculating corresponding tests).

Description

Performs distance correlation sure independence screening (Li et al. 2012) with some additional options (such as calculating corresponding tests).

Usage

```
dcsis(
   X,
   Y,
   k = floor(nrow(X)/log(nrow(X))),
   threshold = NULL,
   calc.cor = "spearman",
   calc.pvalue.cor = FALSE,
   return.data = FALSE,
   test = "none",
   adjustp = "none",
   b = 499,
   bias.corr = FALSE,
   use = "all",
   algorithm = "auto"
)
```

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Arguments

Χ A dataframe or matrix. Υ A vector-valued response having the same length as the number of rows of X. k Number of variables that are selected (only used when threshold is not provided). If provided, variables with a distance correlation larger than threshold are sethreshold lected. calc.cor If set as "pearson", "spearman" or "kendall", a corresponding correlation matrix is additionally calculated. calc.pvalue.cor logical; IF TRUE, a p-value based on the Pearson or Spearman correlation matrix is calculated (not implemented for calc.cor = "kendall") using Hmisc::rcorr. return.data logical; specifies if the dematrix object should contain the original data. test Allows for additionally calculating a test based on distance Covariance. Specifies the type of test that is performed, "permutation" performs a Monte Carlo Permutation test. "gamma" performs a test based on a gamma approximation of the test statistic under the null. "conservative" performs a conservative twomoment approximation. "bb3" performs a quite precise three-moment approximation and is recommended when computation time is not an issue. If setting this parameter to "holm", "hochberg", "hommel", "bonferroni", "BH", adjustp "BY" or "fdr", corresponding adjusted p-values are additionally returned for the distance covariance test. b specifies the number of random permutations used for the permutation test. Ignored for all other tests. logical; specifies if the bias corrected version of the sample distance covariance bias.corr (Huo and Szekely 2016) should be calculated. "all" uses all observations, "complete.obs" excludes NAs, "pairwise.complete.obs" use uses pairwise complete observations for each comparison. algorithm specifies the algorithm used for calculating the distance covariance. (2016).

"fast" uses an O(n log n) algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely

"memsave" uses a memory saving version of the standard algorithm with computational complexity O(n^2) but requiring only O(n) memory.

"standard" uses the classical algorithm. User-specified metrics always use the classical algorithm.

"auto" chooses the best algorithm for the specific setting using a rule of thumb. "memsave" is typically very inefficient for desis and should only be applied in exceptional cases.

Value

dematrix object with the following two additional slots:

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```
name selected description indices of selected variables. name dcor.selected
```

distance correlation of the selected variables and the response Y.

References

Berschneider G, Bottcher B (2018). "On complex Gaussian random fields, Gaussian quadratic forms and sample distance multivariance." *arXiv preprint arXiv:1808.07280*. Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*, **20**, 2305–2330.

Huang C, Huo X (2017). "A statistically and numerically efficient independence test based on random projections and distance covariance." *arXiv preprint arXiv:1701.06054*.

Huo X, Szekely GJ (2016). "Fast computing for distance covariance." *Technometrics*, **58**(4), 435–447.

Li R, Zhong W, Zhu L (2012). "Feature screening via distance correlation learning." *Journal of the American Statistical Association*, **107**(499), 1129–1139.

Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X <- matrix(rnorm(1e5), ncol = 1000)
Y <- sapply(1:100, function(u) sum(X[u, 1:50])) + rnorm(100)
a <- dcsis(X, Y)</pre>
```

distcor

Calculates the distance correlation (Szekely et al. 2007; Szekely and Rizzo 2009).

Description

Calculates the distance correlation (Szekely et al. 2007; Szekely and Rizzo 2009).

Usage

```
distcor(
   X,
   Y,
   affine = FALSE,
   standardize = FALSE,
   bias.corr = FALSE,
   type.X = "sample",
   type.Y = "sample",
   metr.X = "euclidean",
```

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```
metr.Y = "euclidean",
  use = "all",
  algorithm = "auto"
)
```

Arguments

Χ contains either the first sample or its corresponding distance matrix.

> In the first case, X can be provided either as a vector (if one-dimensional), a matrix or a data.frame (if two-dimensional or higher).

> In the second case, the input must be a distance matrix corresponding to the sample of interest.

> If X is a sample, type.X must be specified as "sample". If X is a distance matrix, type.X must be specified as "distance".

Υ see X.

affine logical; specifies if the affinely invariant distance correlation (Dueck et al. 2014)

should be calculated or not.

standardize logical; specifies if X and Y should be standardized dividing each component

by its standard deviations. No effect when affine = TRUE.

bias.corr logical; specifies if the bias corrected version of the sample distance correlation

(Huo and Szekely 2016) should be calculated.

type.X For "distance", X is interpreted as a distance matrix. For "sample", X is inter-

preted as a sample.

type.Y see type.X.

metr.X specifies the metric which should be used to compute the distance matrix for X

(ignored when type.X = "distance").

Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaussauto", "boundsq" or user-specified metrics (see examples).

For "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric, parameter)", e.g. c("gaussian", 3) for a Gaussian metric with bandwidth parameter 3; the default parameter is 2 for "minkowski" and "1" for all other metrics.

See Lyons (2013); Sejdinovic et al. (2013); Bottcher et al. (2018) for details.

metr.Y see metr.X.

specifies how to treat missing values. "complete.obs" excludes observations use

containing NAs, "all" uses all observations.

algorithm specifies the algorithm used for calculating the distance correlation.

> "fast" uses an O(n log n) algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely (2016).

> "memsave" uses a memory saving version of the standard algorithm with computational complexity $O(n^2)$ but requiring only O(n) memory.

> "standard" uses the classical algorithm. User-specified metrics always use the classical algorithm.

> "auto" chooses the best algorithm for the specific setting using a rule of thumb.

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Value

numeric; the distance correlation between samples X and Y.

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*, **20**, 2305–2330.

Huo X, Szekely GJ (2016). "Fast computing for distance covariance." *Technometrics*, **58**(4), 435–447.

Lyons R (2013). "Distance covariance in metric spaces." The Annals of Probability, 41, 3284–3305.

Sejdinovic D, Sriperumbudur B, Gretton A, Fukumizu K (2013). "Equivalence of distance-based and RKHS-based statistics in hypothesis testing." *The Annals of Statistics*, **41**, 2263–2291.

Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X <- rnorm(200)
Y <- rnorm(200)
Z <- X + rnorm(200)
dim(X) <- dim(Y) <- dim(Z) <- c(20, 10)

#Demonstration that biased-corrected distance correlation is #often more meaningful than without using bias-correction

distcor(X, Y)
distcor(X, Z)
distcor(X, Y, bias.corr = TRUE)
distcor(X, Z, bias.corr = TRUE)

#For more examples of the different options,
#see the documentation of distcov.</pre>
```

distcov

Calculates the distance covariance (Szekely et al. 2007; Szekely and Rizzo 2009).

Description

Calculates the distance covariance (Szekely et al. 2007; Szekely and Rizzo 2009).

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Usage

```
distcov(
   X,
   Y,
   affine = FALSE,
   standardize = FALSE,
   bias.corr = FALSE,
   type.X = "sample",
   type.Y = "sample",
   metr.X = "euclidean",
   metr.Y = "euclidean",
   use = "all",
   algorithm = "auto"
)
```

Arguments

X contains either the first sample or its corresponding distance matrix.

In the first case, X can be provided either as a vector (if one-dimensional), a matrix or a data.frame (if two-dimensional or higher).

In the second case, the input must be a distance matrix corresponding to the sample of interest.

If X is a sample, type.X must be specified as "sample". If X is a distance matrix, type.X must be specified as "distance".

Y see X.

affine logical; specifies if the affinely invariant distance covariance (Dueck et al. 2014)

should be calculated or not.

 $standardize \qquad logical; \ specifies \ if \ X \ and \ Y \ should \ be \ standardized \ dividing \ each \ component$

by its standard deviations. No effect when affine = TRUE.

bias.corr logical; specifies if the bias corrected version of the sample distance covariance

(Huo and Szekely 2016) should be calculated.

type.X For "distance", X is interpreted as a distance matrix. For "sample", X is inter-

preted as a sample.

type.Y see type.X.

metr. X specifies the metric which should be used to compute the distance matrix for X

(ignored when type.X = "distance").

Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaus-

sauto", "boundsq" or user-specified metrics (see examples).

For "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric, parameter)", e.g. c("gaussian", 3) for a Gaussian metric with bandwidth parameter 3; the default parameter is 2

for "minkowski" and "1" for all other metrics.

See Lyons (2013); Sejdinovic et al. (2013); Bottcher et al. (2018) for details.

metr.Y see metr.X.

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use specifies how to treat missing values. "complete.obs" excludes observations

containing NAs, "all" uses all observations.

algorithm specifies the algorithm used for calculating the distance covariance.

"fast" uses an O(n log n) algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely (2016).

"memsave" uses a memory saving version of the standard algorithm with computational complexity $O(n^2)$ but requiring only O(n) memory.

"standard" uses the classical algorithm. User-specified metrics always use the classical algorithm.

"auto" chooses the best algorithm for the specific setting using a rule of thumb.

Value

numeric; the distance covariance between samples X and Y.

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*, **20**, 2305–2330.

Huo X, Szekely GJ (2016). "Fast computing for distance covariance." *Technometrics*, **58**(4), 435–447.

Lyons R (2013). "Distance covariance in metric spaces." *The Annals of Probability*, **41**, 3284–3305.

Sejdinovic D, Sriperumbudur B, Gretton A, Fukumizu K (2013). "Equivalence of distance-based and RKHS-based statistics in hypothesis testing." *The Annals of Statistics*, **41**, 2263–2291.

Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X <- rnorm(100)
Y <- X + 3 * rnorm(100)
distcov(X, Y) # standard distance covariance

distcov(X, Y, metr.X = "gaussauto", metr.Y = "gaussauto")
# Gaussian distance with bandwidth choice based on median heuristic

distcov(X, Y, metr.X = c("alpha", 0.5), metr.Y = c("alpha", 0.5))
# alpha distance covariance with alpha = 0.5.

#Define a user-specified (slow) version of the alpha metric</pre>
```

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```
alpha_user <- function(X, prm = 1, kernel = FALSE) {</pre>
    as.matrix(dist(X)) ^ prm
}
distcov(X, Y, metr.X = c("alpha", 0.5), metr.Y = c("alpha", 0.5))
# Gives the same result as before.
#User-specified Gaussian kernel function
gauss_kernel <- function(X, prm = 1, kernel = TRUE) {</pre>
    exp(as.matrix(dist(X)) ^ 2 / 2 / prm ^ 2)
distcov(X, Y, metr.X = c("gauss_kernel", 2), metr.Y = c("gauss_kernel", 2))
# calculates the distance covariance using the corresponding kernel-induced metric
distcov(X, Y, metr.X = c("gaussian", 2), metr.Y = c("gaussian", 2))
# same result
Y <- matrix(nrow = 100, ncol = 2)
X <- rnorm(300)
dim(X) <- c(100, 3)
Z \leftarrow rnorm(100)
Y <- matrix(nrow = 100, ncol = 2)
Y[, 1] \leftarrow X[, 1] + Z
Y[, 2] <- 3 * Z
distcov(X, Y)
distcov(X, Y, affine = TRUE)
# affinely invariant distance covariance
distcov(X, Y, standardize = TRUE)
\#\# distance covariance standardizing the components of X and Y
```

distcov.test

Performs a distance covariance test.

Description

Performs a distance covariance test.

Usage

```
distcov.test(
   X,
   Y,
```

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```
method = "permutation",
 b = 499L
  ln = 20,
 affine = FALSE,
  standardize = FALSE,
 bias.corr = FALSE,
  type.X = "sample",
  type.Y = "sample",
 metr.X = "euclidean",
 metr.Y = "euclidean",
 use = "all",
  return.data = FALSE,
  algorithm = "auto"
)
```

Arguments

Χ

contains either the first sample or its corresponding distance matrix.

In the first case, X can be provided either as a vector (if one-dimensional), a matrix or a data.frame (if two-dimensional or higher).

In the second case, the input must be a distance matrix corresponding to the sample of interest.

If X is a sample, type.X must be specified as "sample". If X is a distance matrix, type.X must be specified as "distance".

Υ

see X.

method

specifies the type of test that is performed.

"permutation" performs a Monte Carlo Permutation test.

"gamma" performs a test based on a gamma approximation of the test statistic under the null (Huang and Huo 2017). This test tends to be anti-conservative, if the "real" p-value is small

"conservative" performs a conservative two-moment approximation (Berschneider and Bottcher 2018).

"bb3" performs a three-moment approximation (Berschneider and Bottcher 2018). This is the most precise parametric option, but only available with the standard algorithm.

"wildbs1" and "wilbs2" perform wild bootstrap tests (Chwialkowski et al. 2014); experimental at the moment.

b

integer; specifies the number of random permutations/bootstrap samples used for the permutation or wild bootstraps tests. Ignored for other tests.

ln

numeric; block size parameter for wild bootstrap tests. Ignored for other tests.

affine

logical; specifies if the affinely invariant distance covariance (Dueck et al. 2014) should be calculated or not.

standardize

logical; specifies if X and Y should be standardized dividing each component by its standard deviations. No effect when affine = TRUE.

bias.corr

logical; specifies if the bias corrected version of the sample distance covariance (Huo and Szekely 2016) should be calculated.

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type.X For "distance", X is interpreted as a distance matrix. For "sample", X is inter-

preted as a sample.

type.Y see type.X.

metr. X specifies the metric which should be used to compute the distance matrix for X

(ignored when type.X = "distance").

Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaus-

sauto", "boundsq" or user-specified metrics (see examples).

For "alpha", "minkowski", "gauss", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric, parameter)", c("gaussian", 3) for example uses a Gaussian metric with bandwidth parameter 3; the default parameter is 2 for "minkowski" and "1" for all other metrics.

See Lyons (2013); Sejdinovic et al. (2013); Bottcher et al. (2018) for details.

metr.Y see metr.X.

use specifies how to treat missing values. "complete.obs" excludes NAs, "all" uses

all observations.

return.data logical; specifies if the test object should contain the original data.

algorithm specifies the algorithm used for calculating the distance covariance.

"fast" uses an $O(n \log n)$ algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely

(2016).

"memsave" uses a memory saving version of the standard algorithm with computational complexity $O(n^2)$ but requiring only O(n) memory.

"standard" uses the classical algorithm. User-specified metrics always use the

classical algorithm.

"auto" chooses the best algorithm for the specific setting using a rule of thumb.

Value

distcov.test object

References

Berschneider G, Bottcher B (2018). "On complex Gaussian random fields, Gaussian quadratic forms and sample distance multivariance." *arXiv preprint arXiv:1808.07280*.

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

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Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." The Annals of Applied Statistics, 3, 1236-1265.

distsd

Calculates the distance standard deviation (Edelmann et al. 2020).

Description

Calculates the distance standard deviation (Edelmann et al. 2020).

Usage

```
distsd(
  Χ,
  affine = FALSE,
  standardize = FALSE,
  bias.corr = FALSE,
  type.X = "sample",
  metr.X = "euclidean",
  use = "all",
  algorithm = "auto"
)
```

Arguments

Χ	contains either the sample or its corresponding distance matrix.
	In the first one V are be associated either as a sector (if one

In the first case, X can be provided either as a vector (if one-dimensional), a matrix or a data.frame (if two-dimensional or higher).

In the second case, the input must be a distance matrix corresponding to the sample of interest.

If X is a sample, type.X must be specified as "sample". If X is a distance matrix,

type.X must be specified as "distance".

affine logical; specifies if the affinely invariant distance standard deviation (Dueck et

al. 2014) should be calculated or not.

logical; specifies if X and Y should be standardized dividing each component standardize

by its standard deviations. No effect when affine = TRUE.

logical; specifies if the bias corrected version of the sample distance standard bias.corr

deviation (Huo and Szekely 2016) should be calculated.

type.X For "distance", X is interpreted as a distance matrix. For "sample", X is inter-

preted as a sample.

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metr.X

specifies the metric which should be used to compute the distance matrix for X (ignored when type.X = "distance").

Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaussauto", "boundsq" or user-specified metrics (see examples).

For "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric, parameter)", e.g. c("gaussian", 3) for a Gaussian metric with bandwidth parameter 3; the default parameter is 2 for "minkowski" and "1" for all other metrics.

See Lyons (2013); Sejdinovic et al. (2013); Bottcher et al. (2018) for details.

use

specifies how to treat missing values. "complete.obs" excludes observations containing NAs, "all" uses all observations.

algorithm

specifies the algorithm used for calculating the distance standard deviation.

"fast" uses an O(n log n) algorithm if the observations are one-dimensional and metr.X and metr.Y are either "euclidean" or "discrete", see also Huo and Szekely (2016).

"memsave" uses a memory saving version of the standard algorithm with computational complexity $O(n^2)$ but requiring only O(n) memory.

"standard" uses the classical algorithm. User-specified metrics always use the classical algorithm.

"auto" chooses the best algorithm for the specific setting using a rule of thumb.

Value

numeric; the distance standard deviation of X.

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

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Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

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Examples

```
X \leftarrow \mathsf{rnorm}(100) distsd(X) # for more examples on the options see the documentation of distcov.
```

extract_np

Extract the dimensions of X.

Description

Extract the dimensions of X.

Usage

```
extract_np(X, type.X)
```

Arguments

X a numeric vector or a numeric matrix.

type.X

either "sample" or "distance". If type.X = "sample", X must be a numeric vector or numeric matrix with the corresponding observations. If metr.X = "distance", X must be a distance matrix.

Value

The centralized distance matrix corresponding to X.

hsplot

Plots Pearson/Spearman/Kendall correlation against distance correlation (often resembling a horseshoe(hs)).

Description

Plots Pearson/Spearman/Kendall correlation against distance correlation (often resembling a horse-shoe(hs)).

Usage

```
hsplot(dcmat, maxcomp = 1e+05, col = "blue", alpha = 1, cortrafo = "none")
```

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Arguments

dcmat A dcmatrix object.

maxcomp Maximum number of associations, for which distance correlation is plotted

against correlation. If the number of associations in the dcmat object is larger, only the maxcomp associations with the largest difference between distance correlation and absolute (Pearson/Spearman/Kendall) correlation are plotted.

col color of the plot.

alpha alpha parameter of the plot.

cortrafo Either "none" or "gaussiandcor". If "gaussiandcor", the distance correlation un-

der assumption of normality is calculated and plotted against the actual distance

correlation.

Note that this is only sensible for Pearson correlation!

Value

Plot of (possibly transformed) Pearson/Spearman/Kendall correlation against distance correlation.

ipcw.dcor Calculates an inverse-probability-of-censoring weighted (IPCW) distance correlation based on IPCW U-statistics (Datta et al. 2010).

Description

Calculates an inverse-probability-of-censoring weighted (IPCW) distance correlation based on IPCW U-statistics (Datta et al. 2010).

Usage

```
ipcw.dcor(
   Y,
   X,
   affine = FALSE,
   standardize = FALSE,
   timetrafo = "none",
   type.X = "sample",
   metr.X = "euclidean",
   use = "all",
   cutoff = NULL
)
```

Arguments

Y A matrix with two columns, where the first column contains the survival times and the second column the status indicators (a survival object will work).

X A vector or matrix containing the covariate information.

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affine logical; specifies if X should be transformed such that the result is invariant under affine transformations of X logical; should X be standardized using the standard deviations of single obserstandardize vations?. No effect when affine = TRUE. timetrafo specifies a transformation applied on the follow-up times. Can be "none", "log" or a user-specified function. For "distance", X is interpreted as a distance matrix. For "sample", X is intertype.X preted as a sample. metr.X specifies the metric which should be used to compute the distance matrix for X (ignored when type.X = "distance"). Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaussauto", "boundsq" or user-specified metrics (see examples). For "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric,parameter)", c("gaussian",3) for example uses a Gaussian metric with bandwidth parameter 3; the default parameter is 2 for "minkowski" and "1" for all other metrics. use specifies how to treat missing values. "complete.obs" excludes observations containing NAs, "all" uses all observations. If provided, all survival times larger than cutoff are set to the cutoff and all corcutoff responding status indicators are set to one. Under most circumstances, choosing a cutoff is highly recommended.

Value

An inverse-probability of censoring weighted estimate for the distance correlation between X and the survival times.

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Datta S, Bandyopadhyay D, Satten GA (2010). "Inverse Probability of Censoring Weighted U-statistics for Right-Censored Data with an Application to Testing Hypotheses." *Scandinavian Journal of Statistics*, **37**(4), 680–700.

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Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

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Examples

```
X <- rnorm(100)
survtime <- rgamma(100, abs(X))
cens <- rexp(100)
status <- as.numeric(survtime < cens)
time <- sapply(1:100, function(u) min(survtime[u], cens[u]))
surv <- cbind(time, status)
ipcw.dcor(surv, X)</pre>
```

ipcw.dcov

Calculates an inverse-probability-of-censoring weighted (IPCW) distance covariance based on IPCW U-statistics (Datta et al. 2010).

Description

Calculates an inverse-probability-of-censoring weighted (IPCW) distance covariance based on IPCW U-statistics (Datta et al. 2010).

Usage

```
ipcw.dcov(
   Y,
   X,
   affine = FALSE,
   standardize = FALSE,
   timetrafo = "none",
   type.X = "sample",
   metr.X = "euclidean",
   use = "all",
   cutoff = NULL
)
```

Arguments

Υ	A column with two rows, where the first row contains the survival times and the second row the status indicators (a survival object will work).
Χ	A vector or matrix containing the covariate information.
affine	logical; indicates if X should be transformed such that the result is invariant under affine transformations of X
standardize	logical; should X be standardized using the standard deviations of single observations?. No effect when affine = TRUE.
timetrafo	specifies a transformation applied on the follow-up times. Can be "none", "log" or a user-specified function.
type.X	For "distance", X is interpreted as a distance matrix. For "sample" (or any other value), X is interpreted as a sample

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metr.X specifies the metric which should be used for X to analyze the distance covariance. Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq". For "alpha", "minkowski", "gauss", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric,parameter)" (see examples); the standard parameter is 2 for "minkowski" and "1" for all other metrics.

use specifies how to treat missing values. "complete.obs" excludes observations containing NAs, "all" uses all observations.

cutoff If provided, all survival times larger than cutoff are set to the cutoff and all cor-

responding status indicators are set to one. Under most circumstances, choosing

a cutoff is highly recommended.

Value

An inverse-probability of censoring weighted estimate for the distance covariance between X and the survival times.

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Datta S, Bandyopadhyay D, Satten GA (2010). "Inverse Probability of Censoring Weighted U-statistics for Right-Censored Data with an Application to Testing Hypotheses." *Scandinavian Journal of Statistics*, **37**(4), 680–700.

Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*. **20**, 2305–2330.

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Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X <- rnorm(100)
survtime <- rgamma(100, abs(X))
cens <- rexp(100)
status <- as.numeric(survtime < cens)
time <- sapply(1:100, function(u) min(survtime[u], cens[u]))
surv <- cbind(time, status)
ipcw.dcov(surv, X)</pre>
```

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ipcw.dcov.test

Performs a permutation test based on the IPCW distance covariance.

Description

Performs a permutation test based on the IPCW distance covariance.

Usage

```
ipcw.dcov.test(
   Y,
   X,
   affine = FALSE,
   standardize = FALSE,
   timetrafo = "none",
   type.X = "sample",
   metr.X = "euclidean",
   use = "all",
   cutoff = NULL,
   B = 499
)
```

Arguments

Υ	A column with two rows, where the first row contains the survival times and the second row the status indicators (a survival object will work).
Χ	A vector or matrix containing the covariate information.
affine	logical; indicates if X should be transformed such that the result is invariant under affine transformations of X.
standardize	logical; should X be standardized using the standard deviations of single observations. No effect when affine = TRUE.
timetrafo	specifies a transformation applied on the follow-up times. Can be "none", "log" or a user-specified function.
type.X	For "distance", X is interpreted as a distance matrix. For "sample" (or any other value), X is interpreted as a sample.
metr.X	metr.X specifies the metric which should be used for X to analyze the distance covariance. Options are "euclidean", "discrete", "alpha", "minkowski", "gaussian", "gaussauto" and "boundsq". For "alpha", "minkowski", "gauss", "gaussauto" and "boundsq", the corresponding parameters are specified via "c(metric,parameter)" (see examples); the standard parameter is 2 for "minkowski" and "1" for all other metrics.
use	specifies how to treat missing values. "complete.obs" excludes observations

containing NAs, "all" uses all observations.

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cutoff If provided, all survival times larger than cutof	If provided, all survival times larger than cutoff are set to the cutoff and all cor-
	responding status indicators are set to one. Under most circumstances, choosing

a cutoff is highly recommended.

B The number of permutations used for the permutation test

Value

An list with two arguments, \$dcov contains the IPCW distance covariance, \$pvalue the corresponding p-value

References

Bottcher B, Keller-Ressel M, Schilling RL (2018). "Detecting independence of random vectors: generalized distance covariance and Gaussian covariance." *Modern Stochastics: Theory and Applications*, **3**, 353–383.

Datta S, Bandyopadhyay D, Satten GA (2010). "Inverse Probability of Censoring Weighted U-statistics for Right-Censored Data with an Application to Testing Hypotheses." *Scandinavian Journal of Statistics*, **37**(4), 680–700.

Dueck J, Edelmann D, Gneiting T, Richards D (2014). "The affinely invariant distance correlation." *Bernoulli*, **20**, 2305–2330.

Huo X, Szekely GJ (2016). "Fast computing for distance covariance." *Technometrics*, **58**(4), 435–447.

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Sejdinovic D, Sriperumbudur B, Gretton A, Fukumizu K (2013). "Equivalence of distance-based and RKHS-based statistics in hypothesis testing." *The Annals of Statistics*, **41**, 2263–2291.

Szekely GJ, Rizzo ML, Bakirov NK (2007). "Measuring and testing dependence by correlation of distances." *The Annals of Statistics*, **35**, 2769–2794.

Szekely GJ, Rizzo ML (2009). "Brownian distance covariance." *The Annals of Applied Statistics*, **3**, 1236–1265.

Examples

```
X <- rnorm(100)
survtime <- rgamma(100, abs(X))
cens <- rexp(100)
status <- as.numeric(survtime < cens)
time <- sapply(1:100, function(u) min(survtime[u], cens[u]))
surv <- cbind(time, status)
ipcw.dcov.test(surv, X)
ipcw.dcov.test(surv, X, cutoff = quantile(time, 0.8))
# often better performance when using a cutoff time</pre>
```

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plot.dcmatrix	Plots a heatmap from a dcmatrix object using the function "pheatmap" from the package "pheatmap".

Description

Plots a heatmap from a dcmatrix object using the function "pheatmap" from the package "pheatmap".

Usage

```
## S3 method for class 'dcmatrix'
plot(
    x,
    type = "dcor",
    trunc.up = NULL,
    trunc.low = NULL,
    cluster_rows = FALSE,
    cluster_cols = FALSE,
    display_numbers = TRUE,
    ...
)
```

Arguments

Value

a heatmap plotting the entries of the slot specified in type of the object specified in dcmat.

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