

# Package ‘BayesSampling’

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**Type** Package

**Title** Bayes Linear Estimators for Finite Population

**Version** 1.1.0

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**Description** Allows the user to apply the Bayes Linear approach to finite population with the Simple Random Sampling - BLE\_SRS() - and the Stratified Simple Random Sampling design - BLE\_SSRS() - (both without replacement), to the Ratio estimator (using auxiliary information) - BLE\_Ratio() - and to categorical data - BLE\_Categorical(). The Bayes linear estimation approach is applied to a general linear regression model for finite population prediction in BLE\_Reg() and it is also possible to achieve the design based estimators using vague prior distributions. Based on Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014) <<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>>.

**URL** <https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>,  
<https://github.com/pedrosfig/BayesSampling>

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.1.1

**Depends** R (>= 3.5)

**Imports** MASS, Matrix, stats, matrixcalc

**Suggests** knitr, rmarkdown, TeachingSampling

**VignetteBuilder** knitr

**Language** en-US

**NeedsCompilation** no

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BigCity

*Full Person-level Population Database*

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## Description

This data set corresponds to some socioeconomic variables from 150266 people of a city in a particular year.

## Usage

```
data(BigCity)
```

## Format

A data.frame with 150266 rows and 12 variables:

**HHID** The identifier of the household. It corresponds to an alphanumeric sequence (four letters and five digits).

**PersonID** The identifier of the person within the household. NOTE it is not a unique identifier of a person for the whole population. It corresponds to an alphanumeric sequence (five letters and two digits).

**Stratum** Households are located in geographic strata. There are 119 strata across the city.

**PSU** Households are clustered in cartographic segments defined as primary sampling units (PSU). There are 1664 PSU and they are nested within strata.

**Zone** Segments clustered within strata can be located within urban or rural areas along the city.

**Sex** Sex of the person.

**Income** Per capita monthly income.

**Expenditure** Per capita monthly expenditure.

**Employment** A person's employment status.

**Poverty** This variable indicates whether the person is poor or not. It depends on income.

### Source

<https://CRAN.R-project.org/package=TeachingSampling>

### References

Package 'TeachingSampling'; see [BigCity](#)

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BLE_Categorical	<i>Bayes Linear Method for Categorical Data</i>
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### Description

Creates the Bayes Linear Estimator for Categorical Data

### Usage

```
BLE_Categorical(ys, n, N, m = NULL, rho = NULL)
```

### Arguments

ys	k-vector of sample proportion for each category.
n	sample size.
N	total size of the population.
m	k-vector with the prior proportion of each strata. If NULL, sample proportion for each strata will be used (non-informative prior).
rho	matrix with the prior correlation coefficients between two different units within categories. It must be a symmetric square matrix of dimension k (or k-1). If NULL, non-informative prior will be used.

### Value

A list containing the following components:

- `est.prop` - BLE for the sample proportion of each category
- `Vest.prop` - Variance associated with the above
- `Vs.Matrix` -  $V_s$  matrix, as defined by the BLE method (should be a positive-definite matrix)
- `R.Matrix` -  $R$  matrix, as defined by the BLE method (should be a positive-definite matrix)

**Source**

<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>

**References**

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

**Examples**

```
# 2 categories
ys <- c(0.2614, 0.7386)
n <- 153
N <- 15288
m <- c(0.7, 0.3)
rho <- matrix(0.1, 1)

Estimator <- BLE_Categorical(ys,n,N,m,rho)
Estimator

ys <- c(0.2614, 0.7386)
n <- 153
N <- 15288
m <- c(0.7, 0.3)
rho <- matrix(0.5, 1)

Estimator <- BLE_Categorical(ys,n,N,m,rho)
Estimator

# 3 categories
ys <- c(0.2, 0.5, 0.3)
n <- 100
N <- 10000
m <- c(0.4, 0.1, 0.5)
mat <- c(0.4, 0.1, 0.1, 0.1, 0.2, 0.1, 0.1, 0.1, 0.6)
rho <- matrix(mat, 3, 3)
```

---

BLE\_Ratio

*Ratio BLE*

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**Description**

Creates the Bayes Linear Estimator for the Ratio "estimator"

**Usage**

```
BLE_Ratio(ys, xs, x_not, m = NULL, v = NULL, sigma = NULL, n = NULL)
```

**Arguments**

<code>ys</code>	vector of sample observations or sample mean (sigma and n parameters will be required in this case).
<code>xs</code>	vector with values for the auxiliary variable of the elements in the sample or sample mean.
<code>x_not</code> s	vector with values for the auxiliary variable of the elements not in the sample.
<code>m</code>	prior mean for the ratio between Y and X. If NULL, $\text{mean}(ys)/\text{mean}(xs)$ will be used (non-informative prior).
<code>v</code>	prior variance of the ratio between Y and X (bigger than $\text{sigma}^2$ ). If NULL, it will tend to infinity (non-informative prior).
<code>sigma</code>	prior estimate of variability (standard deviation) of the ratio within the population. If NULL, sample variance of the ratio will be used.
<code>n</code>	sample size. Necessary only if <code>ys</code> and <code>xs</code> represent sample means (will not be used otherwise).

**Value**

A list containing the following components:

- `est.beta` - BLE of Beta
- `Vest.beta` - Variance associated with the above
- `est.mean` - BLE for each individual not in the sample
- `Vest.mean` - Covariance matrix associated with the above
- `est.tot` - BLE for the total
- `Vest.tot` - Variance associated with the above

**Source**

<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>

**References**

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

**Examples**

```
ys <- c(10,8,6)
xs <- c(5,4,3.1)
x_not
```

s <- c(1,20,13,15,-5)
m <- 2.5
v <- 10
sigma <- 2

Estimator <- BLE\_Ratio(ys, xs, x\_nots, m, v, sigma)
Estimator

```
# Same example but informing sample means and sample size instead of sample observations
ys <- mean(c(10,8,6))
xs <- mean(c(5,4,3.1))
n <- 3
x_notss <- c(1,20,13,15,-5)
m <- 2.5
v <- 10
sigma <- 2

Estimator <- BLE_Ratio(ys, xs, x_notss, m, v, sigma, n)
Estimator
```

---

BLE\_Reg

*General BLE case*


---

### Description

Calculates the Bayes Linear Estimator for Regression models (general case)

### Usage

```
BLE_Reg(ys, xs, a, R, Vs, x_notss, V_notss)
```

### Arguments

ys	response variable of the sample
xs	explicative variable of the sample
a	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_notss	values of X for the individuals not in the sample
V_notss	covariance matrix of the individuals not in the sample

### Value

A list containing the following components:

- est.beta - BLE of Beta
- Vest.beta - Variance associated with the above
- est.mean - BLE of each individual not in the sample
- Vest.mean - Covariance matrix associated with the above
- est.tot - BLE for the total
- Vest.tot - Variance associated with the above

**Source**

<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>

**References**

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

**Examples**

```
xs <- matrix(c(1,1,1,1,2,3,5,0),nrow=4,ncol=2)
ys <- c(12,17,28,2)
x_ots <- matrix(c(1,1,1,0,1,4),nrow=3,ncol=2)
a <- c(1.5,6)
R <- matrix(c(10,2,2,10),nrow=2,ncol=2)
Vs <- diag(c(1,1,1,1))
V_ots <- diag(c(1,1,1))

Estimator <- BLE_Reg(ys, xs, a, R, Vs, x_ots, V_ots)
Estimator
```

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BLE\_SRS

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*Simple Random Sample BLE*


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**Description**

Creates the Bayes Linear Estimator for the Simple Random Sampling design (without replacement)

**Usage**

```
BLE_SRS(ys, N, m = NULL, v = NULL, sigma = NULL, n = NULL)
```

**Arguments**

ys	vector of sample observations or sample mean (sigma and n parameters will be required in this case).
N	total size of the population.
m	prior mean. If NULL, sample mean will be used (non-informative prior).
v	prior variance of an element from the population (bigger than $\sigma^2$ ). If NULL, it will tend to infinity (non-informative prior).
sigma	prior estimate of variability (standard deviation) within the population. If NULL, sample variance will be used.
n	sample size. Necessary only if ys represent sample mean (will not be used otherwise).

**Value**

A list containing the following components:

- `est.beta` - BLE of Beta (BLE for every individual)
- `Vest.beta` - Variance associated with the above
- `est.mean` - BLE for each individual not in the sample
- `Vest.mean` - Covariance matrix associated with the above
- `est.tot` - BLE for the total
- `Vest.tot` - Variance associated with the above

**Source**

<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>

**References**

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. *Survey Methodology*, 40, 15-28.

**Examples**

```
ys <- c(5,6,8)
N <- 5
m <- 6
v <- 5
sigma <- 1

Estimator <- BLE_SRS(ys, N, m, v, sigma)
Estimator

# Same example but informing sample mean and sample size instead of sample observations
ys <- mean(c(5,6,8))
N <- 5
n <- 3
m <- 6
v <- 5
sigma <- 1

Estimator <- BLE_SRS(ys, N, m, v, sigma, n)
Estimator
```



BLE\_SSRS

*Stratified Simple Random Sample BLE***Description**

Creates the Bayes Linear Estimator for the Stratified Simple Random Sampling design (without replacement)

**Usage**

```
BLE_SSRS(ys, h, N, m = NULL, v = NULL, sigma = NULL)
```

**Arguments**

ys	vector of sample observations or sample mean for each strata (sigma parameter will be required in this case).
h	vector with number of observations in each strata.
N	vector with the total size of each strata.
m	vector with the prior mean of each strata. If NULL, sample mean for each strata will be used (non-informative prior).
v	vector with the prior variance of an element from each strata (bigger than $\sigma^2$ for each strata). If NULL, it will tend to infinity (non-informative prior).
sigma	vector with the prior estimate of variability (standard deviation) within each strata of the population. If NULL, sample variance of each strata will be used.

**Value**

A list containing the following components:

- `est.beta` - BLE of Beta (BLE for the individuals in each strata)
- `Vest.beta` - Variance associated with the above
- `est.mean` - BLE for each individual not in the sample
- `Vest.mean` - Covariance matrix associated with the above
- `est.tot` - BLE for the total
- `Vest.tot` - Variance associated with the above

**Source**

<https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886>

**References**

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. *Survey Methodology*, 40, 15-28.

**Examples**

```

ys <- c(2,-1,1.5, 6,10, 8,8)
h <- c(3,2,2)
N <- c(5,5,3)
m <- c(0,9,8)
v <- c(3,8,1)
sigma <- c(1,2,0.5)

Estimator <- BLE_SSRS(ys, h, N, m, v, sigma)
Estimator

# Same example but informing sample means instead of sample observations
y1 <- mean(c(2,-1,1.5))
y2 <- mean(c(6,10))
y3 <- mean(c(8,8))
ys <- c(y1, y2, y3)
h <- c(3,2,2)
N <- c(5,5,3)
m <- c(0,9,8)
v <- c(3,8,1)
sigma <- c(1,2,0.5)

Estimator <- BLE_SSRS(ys, h, N, m, v, sigma)
Estimator

```

---

C *calculates the C factor*

---

**Description**

calculates the C factor

**Usage**

`C(ys, xs, R, Vs)`

**Arguments**

ys	response variable of the sample
xs	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors

---

create1	<i>creates vector of 1's to be used in the estimators</i>
---------	---

---

**Description**

creates vector of 1's to be used in the estimators

**Usage**

create1(y)

**Arguments**

y	sample matrix
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**Value**

vector of 1's with size equal to the number of observations in the sample

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E_beta	<i>calculates the BLE for Beta</i>
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**Description**

calculates the BLE for Beta

**Usage**

E\_beta(ys, xs, a, R, Vs)

**Arguments**

ys	response variable of the sample
xs	explicative variable of the sample
a	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors

---

E\_theta\_Reg                      *calculates the BLE for the individuals not in the sample*

---

### Description

calculates the BLE for the individuals not in the sample

### Usage

E\_theta\_Reg(ys, xs, a, R, Vs, x\_notss)

### Arguments

ys	response variable of the sample
xs	explicative variable of the sample
a	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_notss	values of X for the individuals not in the sample

---

T\_Reg                                *calculates BLE for the total T*

---

### Description

calculates BLE for the total T

### Usage

T\_Reg(ys, xs, a, R, Vs, x\_notss)

### Arguments

ys	response variable of the sample
xs	explicative variable of the sample
a	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_notss	values of X for the individuals not in the sample

---

VT_Reg	<i>calculates risk matrix associated with the BLE for for the total T</i>
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---

**Description**

calculates risk matrix associated with the BLE for for the total T

**Usage**

VT\_Reg(ys, xs, a, R, Vs, x\_not, V\_not)

**Arguments**

ys	response variable of the sample
xs	explicative variable of the sample
a	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_not	values of X for the individuals not in the sample
V_not	covariance matrix of the individuals not in the sample

---

V_beta	<i>calculates the risk matrix associated with the BLE for Beta</i>
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**Description**

calculates the risk matrix associated with the BLE for Beta

**Usage**

V\_beta(ys, xs, R, Vs)

**Arguments**

ys	response variable of the sample
xs	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors

---

V_theta_Reg	<i>calculates the risk matrix associated with the BLE for the individuals not in the sample</i>
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---

**Description**

calculates the risk matrix associated with the BLE for the individuals not in the sample

**Usage**

```
V_theta_Reg(ys, xs, R, Vs, x_not, V_not)
```

**Arguments**

ys	response variable of the sample
xs	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors
x_not	values of X for the individuals not in the sample
V_not	covariance matrix of the individuals not in the sample

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